

WOLKIT

LESSON

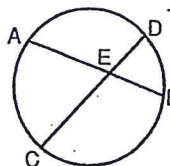
**Review for Mastery**

**11-6**

**Segment Relationships in Circles**

**Chord-Chord Product Theorem**

If two chords intersect in the interior of a circle, then the products of the lengths of the segments of the chords are equal.



$AE \cdot EB = CE \cdot ED$

Find the value of  $x$  and the length of each chord.

$HL \cdot LJ = KL \cdot LM$

Chord-Chord Product Thm.

$4 \cdot 9 = 6 \cdot x$

$HL = 4, LJ = 9, KL = 6, LM = x$

$36 = 6x$

Simplify.

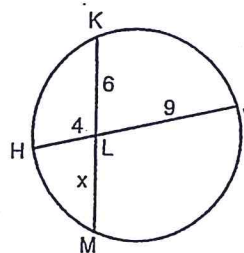
$6 = x$

Divide each side by 6.

$HJ = 4 + 9 = 13$

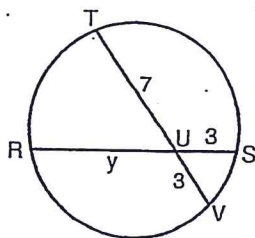
$KM = 6 + x$

$= 6 + 6 = 12$



Find the value of the variable and the length of each chord.

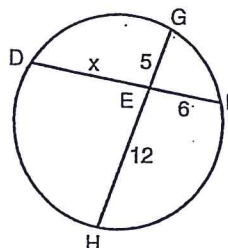
1.



$7 \cdot 3 = y \cdot 3$   
 $7 = y$

$RS = 7 + 3 = 10$      $TV = 7 + 3 = 10$

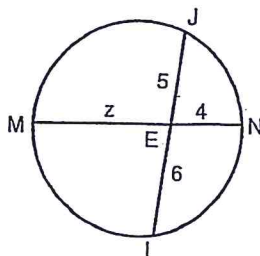
2.



$6x = 5 \cdot 12$   
 $\frac{6x}{6} = \frac{60}{6}$   
 $x = 10$

$DF = 10 + 6 = 16$      $GH = 12 + 5 = 17$

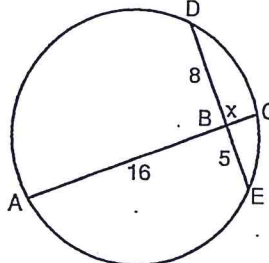
3.



$4z = 5 \cdot 6$   
 $z = 7.5$

$MN = 7.5 + 4 = 11.5$      $JL = 11$

4.



$16x = 8 \cdot 5$   
 $16x = 40$   
 $x = 2.5$

$AC = 16 + 2.5 = 18.5$      $DE = 13$

LESSON

**Review for Mastery**

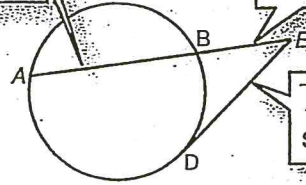
**11-6 Segment Relationships in Circles** continued

- A **secant segment** is a segment of a secant with at least one endpoint on the circle.
- An **external secant segment** is the part of the secant segment that lies in the exterior of the circle.
- A **tangent segment** is a segment of a tangent with one endpoint on the circle.

$\overline{AE}$  is a secant segment.

$\overline{BE}$  is an external secant segment.

$\overline{ED}$  is a tangent segment.

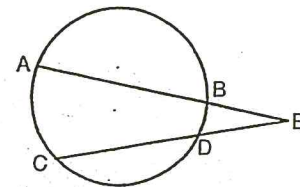


If two segments intersect outside a circle, the following theorems are true.

**Secant-Secant Product Theorem**

The product of the lengths of one secant segment and its external segment equals the product of the lengths of the other secant segment and its external segment.

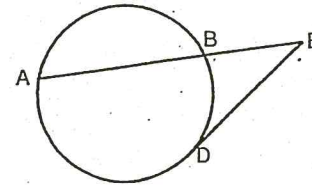
whole • outside = whole • outside  
 $AE \cdot BE = CE \cdot DE$



**Secant-Tangent Product Theorem**

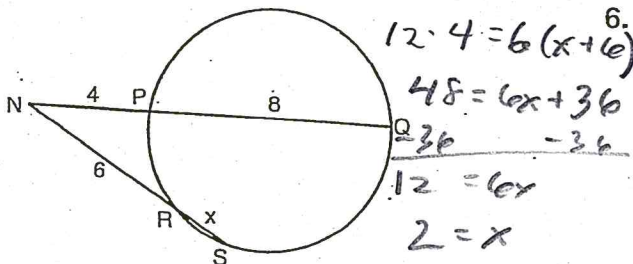
The product of the lengths of the secant segment and its external segment equals the length of the tangent segment squared.

whole • outside = tangent<sup>2</sup>  
 $AE \cdot BE = DE^2$

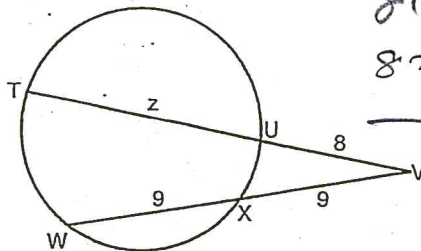


Find the value of the variable and the length of each secant segment.

5.



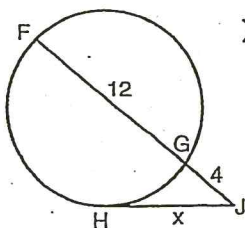
$NQ = 12$   $NS = 8$



$8(z+8) = 18 \cdot 9$   
 $8z + 64 = 162$   
 $\quad -64 \quad -64$   
 $8z = 98$   
 $z = 12.25$

Find the value of the variable.

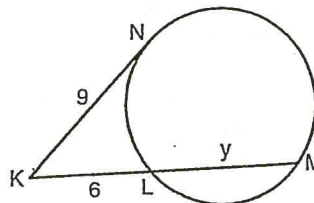
7.



$x^2 = 12 \cdot 4$   
 $x^2 = 48$   
 $x = 8$

$FJ = 16$ ,  $HJ = 8$

8.



$6(y+6) = 9^2$   
 $6y + 36 = 81$   
 $\quad -36 \quad -36$   
 $\frac{6y}{6} = \frac{45}{6}$   
 $y = 7.5$

$KN = 9$   $LM = 13.5$